

## Research article

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# Enhanced broadband absorption in nanowire arrays with integrated Bragg reflectors

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**Abstract:** A near-unity unselective absorption spectrum is desirable for high-performance photovoltaics. Nanowire (NW) arrays are promising candidates for efficient solar cells due to nanophotonic absorption resonances in the solar spectrum. The absorption spectra, however, display undesired dips between the resonance peaks. To achieve improved unselective broadband absorption, we propose to enclose distributed Bragg reflectors (DBRs) in the bottom and top parts of indium phosphide (InP) NWs, respectively. We theoretically show that by enclosing only two periods of  $\text{In}_{0.56}\text{Ga}_{0.44}\text{As}/\text{InP}$  DBRs, an unselective 78% absorption efficiency (72% for NWs without DBRs) is obtained at normal incidence in the spectral range from 300 nm to 920 nm. Under oblique light incidence, the absorption efficiency is enhanced up to about 85% at an incidence angle of  $50^\circ$ . By increasing the number of DBR periods from two to five, the absorption efficiency is further enhanced up to 95% at normal incidence. In this work, we calculated optical spectra for InP NWs, but the results are expected to be valid for other direct band gap III–V semiconductor materials. We believe that our proposed idea of integrating DBRs in NWs offers great potential for high-performance photovoltaic applications.

**Keywords:** light trapping; distributed Bragg reflectors (DBRs); nanowires; photovoltaics.

## 1 Introduction

Nanowire (NW) arrays are intensively investigated for their potential use in photodetectors [1–4] and photovoltaics [5, 6] due to absorption of excited optical modes. In order to optimize the photovoltaic efficiency of NW array solar cells, it is important to engineer and reinforce absorption of the relevant excited optical modes to achieve an enhanced broadband light absorption in the solar spectrum. NWs support resonant optical modes due to their comparable dimensions to optical wavelengths [5, 7, 8]. One well-known strategy to enhance absorption is by tailoring the NW geometry [7–10], e.g. for an identical diameter, by increasing the NW length and decreasing the distance between the NWs (pitch of the array). Such methods, however, lead to significantly increased material consumption. Moreover, the dark current in NW-based solar cells typically increases with NW length, which in turn reduces photovoltaic efficiency [11]. Another strategy to improve the absorption characteristics in NWs is to break the symmetry of the NW array/light incidence system [12]. Invoking oblique light incidence conditions improves absorption due to excitation of new polarization-dependent optical modes [12, 13]. The improvement is, however, limited to relatively narrow regions of the solar spectrum [12]. To obtain further enhanced absorption for identical geometry of the NWs in a broad spectral range, light trapping mechanisms have been invoked to reduce transmission through the NW/substrate interface [5] and light reflection at the superstrate/NW interface [14–16] and to enhance the absorption in the NWs [17–19]. An ultimate strategy would offer strong absorption throughout the solar spectrum; wherefore, novel light trapping mechanisms [20] need to be explored in order to improve the solar cell efficiency [21, 22].

In this theoretical study, we propose to integrate axially distributed DBRs in the NWs as wavelength-selective mirrors that efficiently trap the light inside the NWs and strongly suppress the leakage of light into the substrate [23]. An increased optical path length of the excited modes, due to multiple round trips in the DBR-NWs as a result of multi-reflection from the DBRs, leads to enhanced

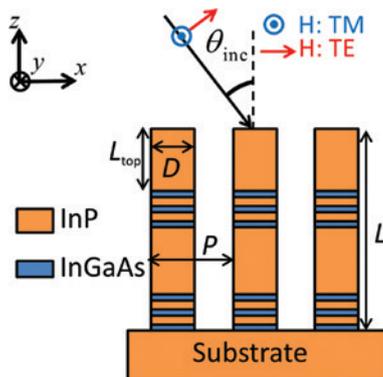
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absorption and enhanced photovoltaic efficiency without the drawbacks of, e.g. increased dark current observed in elongated NWs [11]. Moreover, by properly optimizing the position of DBRs in the NWs, in addition to employing oblique incident light conditions, a near-unity absorption can be achieved throughout most of the solar spectrum. It should be noted that the embedded DBRs might potentially act as traps for the photogenerated charge carriers. In a recent report from our group, we showed, however, that InP NW photodetectors with embedded axial InAsP quantum discs with relatively deep confining potentials along the NWs exhibit excellent electro-optical properties at room temperature [4]. The high electric field strength in a typical p-i-n geometry of the NWs is likely to efficiently collect the photogenerated carriers. The proposed design of realizing integrated DBRs in NWs offers a novel promising route to realize enhanced broadband absorption and photovoltaic efficiency in photodetectors and solar cells.

## 2 Calculations

In this work, we consider square arrays of vertically standing InP NWs containing two absorbing DBRs comprising two (or five) alternating quarter-wave  $\text{In}_{0.56}\text{Ga}_{0.44}\text{As}$ /InP layers. Here, we calculate the absorption spectra for sparse square NW arrays. As the optical absorption of sparse NW arrays does not depend strongly on the lattice arrangement, we believe that the results are valid to a good approximation for other arrangements, like, e.g. hexagonal arrays [12]. Figure 1 shows schematics of the square array with DBR-NWs of diameter ( $D$ ), length ( $L$ ), and pitch ( $P$ ).  $L_{\text{top}}$  is the distance from the top surface of



**Figure 1:** Schematics of a square DBR-NW array with defined H polarization vectors of the TM and TE modes in the plane of incidence.

The blue and orange thin layers depict alternating quarter-wave layers of  $\text{In}_{0.56}\text{Ga}_{0.44}\text{As}$  and InP forming the DBRs.

the NW to the upper DBR. The polar angle  $\theta_{\text{inc}}$  indicates the angle of incidence of the light relative to the NWs. The inset illustrates the geometry for the transverse electric (TE) and transverse magnetic (TM) polarized light. One DBR period consists of layers with refractive indices  $n_{\text{InGaAs}}$  and  $n_{\text{InP}}$  and corresponding thicknesses  $d_{\text{InGaAs}}$  and  $d_{\text{InP}}$ . As the lateral scale of the DBR (equal to the diameter of the NW) is comparable to the wavelength of the incident light, diffraction effects become significant [24, 25]. To take the diffraction effects into account, we perform an analysis of the DBR-NWs based on the finite element numerical method. The thicknesses of the quarter-wave stacked layers are taken as  $d_{\text{InP}} = \lambda_{\text{HE}_{11}\text{InP}} / 4$  and  $d_{\text{InGaAs}} = \lambda_{\text{HE}_{11}\text{InGaAs}} / 4$ , where  $\lambda_{\text{HE}_{11}\text{InP}}$  and  $\lambda_{\text{HE}_{11}\text{InGaAs}}$  are the wavelengths of the fundamental excited  $\text{HE}_{11}$  mode in InP NWs and InGaAs NWs for a given geometrical parameter, respectively [25].

To evaluate the absorption spectra of DBR-NWs under plane wave incidence, we implemented a numerical full-wave finite element method in COMSOL to solve Maxwell's equations. We use perfectly matched layer (PML) boundary conditions in the vertical  $z$ -direction and Floquet boundary conditions in the  $x$ - and  $y$ -direction to construct an infinite periodic square array. The solutions to Maxwell's equations describe the electric field distribution inside and outside of the NWs. The absorption at each wavelength  $\lambda$  over the volume  $V$  of the NW is given by  $A(\lambda) = \frac{1}{2} \int \frac{2\pi\epsilon_0 c}{\lambda} |E(\lambda)|^2 \text{Im}(n^2(\lambda)) dV$  [16], where  $\epsilon_0$  is the vacuum permittivity,  $c$  is the speed of light in vacuum,  $\lambda$  is the photon wavelength,  $E$  is the electric field, and  $n$  is the complex refractive index. Here, the absorption  $A(\lambda)$  is defined as the fraction of incident light absorbed in the NWs at wavelength  $\lambda$ , while the transmission  $T(\lambda)$  is the fraction of incident light transmitted into the substrate. From energy conservation, the reflection is calculated through the relationship  $R(\lambda) = 1 - T(\lambda) - A(\lambda)$ . In our previous studies [9, 10], we have shown that there is a good agreement between the optical response determined from experiments and from calculations based on NW array models similar to that described above. We expect that oblique incident light conditions will result in polarization-dependent absorption spectra. To investigate the effects of incidence angle  $\theta_{\text{inc}}$  on the absorption characteristics, we average the TM and TE absorption spectra and denote the resulting spectrum polarization-averaged. We used tabulated data for refractive indices of InP [26] and  $\text{In}_{0.56}\text{Ga}_{0.44}\text{As}$  [27]. To evaluate the absorption characteristics of the DBR-NWs in the solar spectrum, we calculated the normalized absorption efficiency,  $\eta$ , defined as follows:

$$\eta = \frac{\int_{300}^{\lambda_g} I(\lambda) A(\lambda) \frac{\lambda}{\lambda_g} d\lambda}{\int_{300}^{\lambda_g} I(\lambda) \frac{\lambda}{\lambda_g} d\lambda}, \quad (1)$$

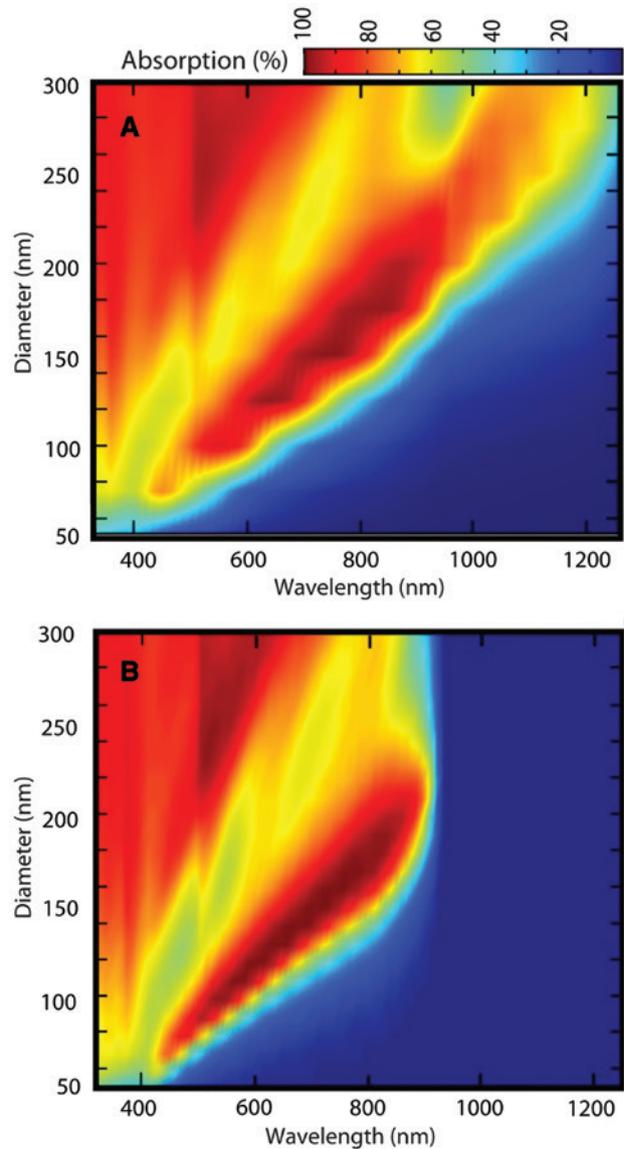
where  $\lambda_g$  is the photon wavelength corresponding to the band gap of InP (920 nm, 1.344 eV).  $I(\lambda)$  is the solar spectral irradiance assuming standard air mass 1.5 (AM1.5) [28]. We chose the spectral range from 300 nm to  $\lambda_g$  in the integration due to the band gap of InP and to the fact that  $I(\lambda)$  is negligible for  $\lambda < 300$  nm. The band gap energy of the  $\text{In}_{0.56}\text{Ga}_{0.44}\text{As}$  layers in the DBRs is set to 0.95 eV (1300 nm).

### 3 Results and discussion

Geometrically tailored NWs have been invoked to enhance the light absorption in NWs in the solar spectrum [6, 16, 29]. One alternative to enhance absorption is by elongating the NWs to completely absorb the guided light inside the NWs (reducing the transmission at the NW/substrate). Besides the obvious disadvantage of increased material consumption, this approach also reduces the photovoltaic efficiency of the solar cell as the dark current is proportional to the length of the NWs. Instead, to reduce the transmission of guided modes into the substrate without elongating the NWs, we consider two DBRs inside the NWs forming an effective light-trapping Fabry-Perot cavity (see Supplementary Figure S1), which elongates the optical path length of the excited modes, thereby enhancing the absorption of the guided modes. We note that possible trapping of carriers by the valence band and conduction band “wells” induced by the DBRs should not impose a significant problem at room temperature, in particular, not for the relatively small offsets in the present case (about 0.25 eV in the conduction band [30–32]) in combination with a high-electric field strength. In fact, in our recent study, we show excellent responsivity in a photodetector with a conduction band offset of 0.40 eV [4].

To broaden the absorption spectra of the NWs, their diameter should be increased to couple a larger number of spectrally different excited modes into the NWs [13]. The optical path length of the fundamental  $\text{HE}_{11}$  mode, however, decreases for thicker NWs (see Supplementary Figure S2), which confines the absorption region of this excited mode to the top part of the NWs [6, 33]. To compensate this and to make sure that the larger refractive index of InGaAs [27] compared to InP [26] would not cause increased reflection of incident light from the top surface of the NWs, we insert the DBRs at a distance of 400 nm

from the top surface of the NW based on the optical path length relation of the  $\text{HE}_{11}$  mode [8]. Here, the optical path length relation is  $1/\alpha$ , where  $\alpha$  is the absorption coefficient of InP. The two DBRs in the respective ends of the NWs each comprise two periods of alternating quarter-wave  $\text{In}_{0.56}\text{Ga}_{0.44}\text{As}$  and InP layers. In order to further increase the reflection from the DBRs, we included an additional high-index  $\text{In}_{0.56}\text{Ga}_{0.44}\text{As}$  terminating layer to the DBRs [25] in the final geometry. We consider the well-established photovoltaic material system InGaAs/InP [3, 34, 35] for the DBRs. More specifically, the composition  $\text{In}_{0.56}\text{Ga}_{0.44}\text{As}$



**Figure 2:** Calculated absorption in NW arrays versus wavelength and NW diameter at normal incidence.

(A) and (B) show NW arrays with and without embedded DBRs, respectively. The geometrical parameters for both panels are  $L = 1100$  nm and  $P = 500$  nm.

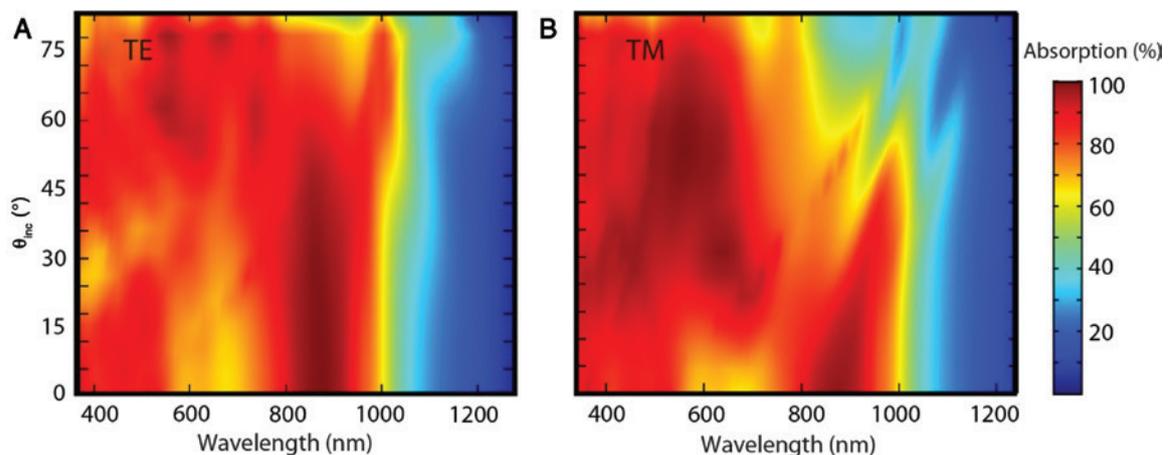
[36] was chosen to optimize the conditions of good lattice matching to InP for future realization of the solar cells and the requirement of a finite index difference in the DBRs [24]. For the NWs, we chose the diameter  $D=200$  nm, total length  $L=1100$  nm (with or without DBRs), and pitch  $P=500$  nm to make sure that no absorption saturation occurs, which can be observed for longer NWs [9, 10] or denser arrays (smaller pitch) of NWs [6, 8, 12].

Figure 2 shows a comparison between absorption spectra of InP NWs and InGaAs/InP NW-DBRs under normal incidence ( $\theta_{\text{inc}}=0^\circ$ ) as a function of  $D$  for identical values of  $P$  and  $L$ . Note that  $L$  accounts for the total length of the NWs, including the DBRs. The results indicate two key points: first, the absorption extends to longer wavelengths by employing DBRs. In particular, the wavelength position of the  $\text{HE}_{11}$  mode extends up to about 1150 nm. The extension originates from the absorbing InGaAs layers in the DBRs (see Supplementary Figure S3). Second, the absorption is improved in NW-DBRs in the middle spectral range (500 nm–800 nm for varying  $D$ ) due to enhanced contributions from the longitudinal Fabry-Perot modes. These longitudinal modes form when the guided modes undergo multiple reflections from the embedded DBRs [8].

Oblique incident light breaks the symmetry of a NW/light incidence system and enhances the absorption in the middle part of the solar spectrum by exciting additional Mie resonances [12, 13]. For NWs without DBRs, however, the excitation of symmetry-dependent guided  $\text{HE}_{1m}$  modes ( $m$  is the radial mode number) becomes weaker in both the longest and shortest wavelength parts of the spectrum [12]. By incorporating top and bottom DBRs in the NWs, we can reinforce both the excitation of  $\text{HE}_{1m}$  modes and Mie resonances and consequently achieve unselective broadband absorption at certain angles of incidence. Figure 3

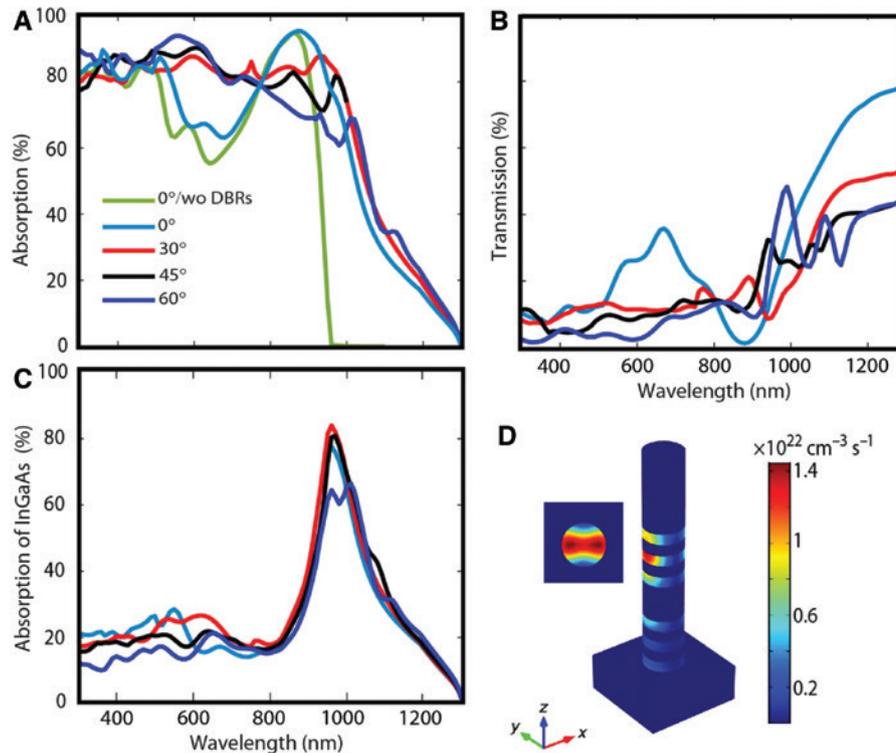
below shows TM- and TE-polarized absorption spectra of DBR-NWs versus incident angle  $\theta_{\text{inc}}$ . It is readily observed that both polarized spectra exhibit an improved absorption over a broad spectral range at certain incident angles compared to normal incidence absorption.

To clearly compare the absorption enhancement versus  $\theta_{\text{inc}}$ , we plot the polarization-averaged absorption spectra of DBR-NWs in Figure 4A. The observed enhancement implies a strong light trapping in the NWs, which effectively reduces the transmission (leakage) of light into the substrate (Figure 4B) while maintaining a more or less constant reflection (not shown). Evidently, the absorption profile around the band gap of InP is significantly broadened upon introducing the InGaAs/InP DBRs, in particular, for  $\theta_{\text{inc}} \leq 45^\circ$  (Figure 4B). To investigate this observation in more detail, we explore separately the absorption properties of the DBRs and especially the InGaAs layers. Figure 4C shows the absorption spectra versus  $\theta_{\text{inc}}$  of the InGaAs layers in the DBRs. A new strong absorption peak at 960 nm is excited, which strongly affects the absorption profile around the band gap energy of InP, leading to the observed broadening effect. Our calculations confirm that the absorption peak at 960 nm stems from reinforced absorption of the fundamental  $\text{HE}_{11}$  mode in the thin InGaAs layers [5] due to multi-reflection from the DBRs. The photon absorption profile for normal incidence at 960 nm, shown in Figure 4D, displays strong light confinement in the InGaAs layers, leading to 390% enhanced absorption from 16% at 800 nm to 78% at 960 nm (Figure 4C). The enhancement at 960 nm can be further boosted up to 83% for oblique incidence at  $\theta_{\text{inc}}=30^\circ$ . The presence of this new strong absorption peak flattens and enhances the absorption spectra of DBR-NWs at long wavelengths ranging from 850 nm to 1000 nm (Figure 4A). Furthermore, calculations show that by increasing the number of DBR periods from 2



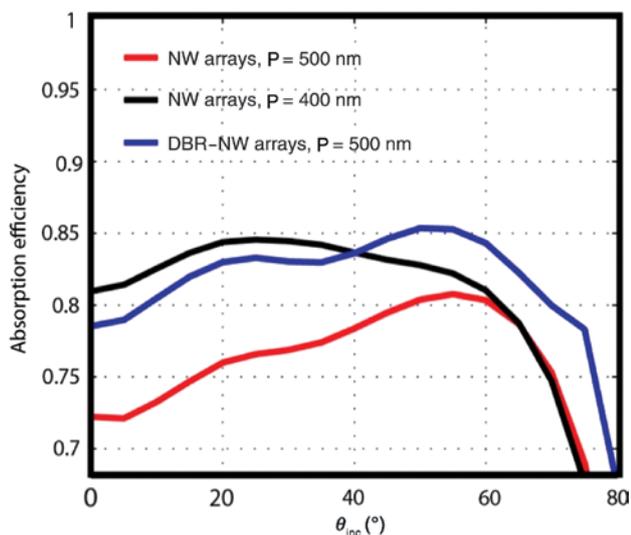
**Figure 3:** Calculated absorption in DBR-NW arrays versus wavelength and angle of incidence.

(A) TE-polarization and (B) TM-polarization. The geometrical parameters are  $D=200$  nm,  $L=1100$  nm, and  $P=500$  nm.



**Figure 4:** Calculated absorption and transmission in DBR-NW arrays versus wavelength and angle of incidence. (A) Polarization-averaged absorption spectra versus light incidence angle ( $\theta_{\text{inc}}$ ) of DBR-NWs. The green trace shows the absorption spectrum of InP arrays without DBRs under normal incidence. (B) Transmission spectra of DBR-NWs versus  $\theta_{\text{inc}}$ . (C) Absorption spectra of the InGaAs layers as a function of  $\theta_{\text{inc}}$ , revealing a strong peak around the band gap wavelength of InP. (D) Photon absorption profile at 960 nm. Inset shows x-y cross section of photon absorption profile in the middle layer of the top DBR (InGaAs layer).

to 5, the absorption at 960 nm at normal incidence can be enhanced from 78% up to 95% at the expense of slightly more absorbing material. This drastic improvement is due



**Figure 5:** Calculated absorption efficiency of DBR-NW arrays with 500-nm pitch (blue trace), and for NW arrays without DBRs with 500-nm pitch (red trace) and 400-nm pitch (black trace), respectively, versus light incidence angle.

to a suppressed light transmission from 20% to merely 3% from the DBR-NWs into the substrate while maintaining a constant low reflection of 2% from the NWs.

Figure 5 shows the effect of light trapping due to DBRs on the enhancement of the absorption efficiency versus  $\theta_{\text{inc}}$ . The results indicate that the absorption efficiency of DBR-NWs with 500-nm pitch (blue trace) exceeds not only that of InP NWs with 400-nm pitch (black trace) for  $\theta_{\text{inc}} > 40^\circ$  but also for all angles of incidence for InP NW arrays with 500-nm pitch (red trace).

## 4 Conclusions

We have theoretically investigated optical absorption in InP NW arrays on InP substrates with integrated  $\text{In}_{0.56}\text{Ga}_{0.44}\text{As}/\text{InP}$  DBRs inside the wires forming a resonant Fabry-Perot cavity. Detailed calculations show that an unselective 85% light absorption efficiency in the range  $300 \text{ nm} < \lambda < 920 \text{ nm}$  can be achieved in optimized array structures at  $50^\circ$  oblique light incidence. The DBR-NW arrays have the main advantage of small transmission (leakage) of light into the substrate due to strong light

trapping provided by DBRs. The light trapping due to multiple reflections from the DBRs effectively increases the optical path length of the excited modes in the NWs and enhances the absorption efficiency. A key feature underlying the significantly enhanced and broadened absorption profile is the appearance of an additional fundamental mode at 960 nm, which leads to both a strong absorption in the InGaAs layers and strongly modified absorption properties around the band gap energy of InP. Here we calculated optical spectra for InP NWs, but the results are expected to be valid for other direct band gap III–V semiconductor materials. We believe that our proposed idea of integrating DBRs in NWs offers great potential for new types of high-performance photovoltaic applications.

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